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# Computing minimal mappings

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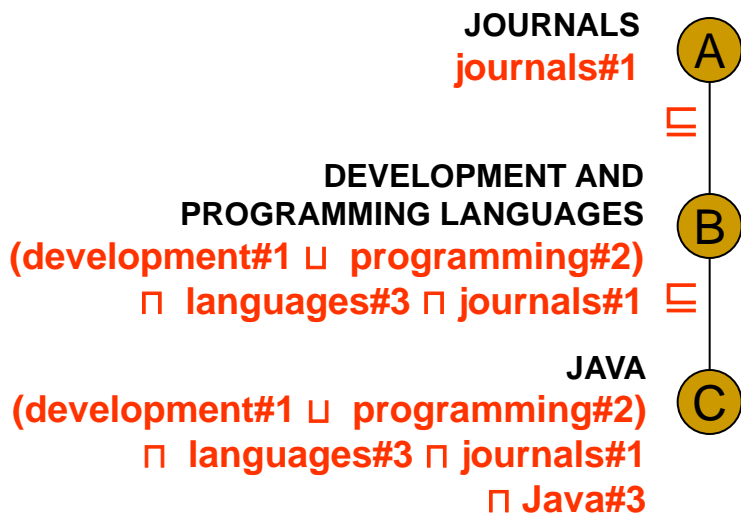
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# Roadmap

- Lightweight ontologies
- Mapping and minimal mapping
  - Computing a mapping: **SMatch**
  - Computing the minimal mapping: **MinSMatch**
- Evaluation
- Conclusions

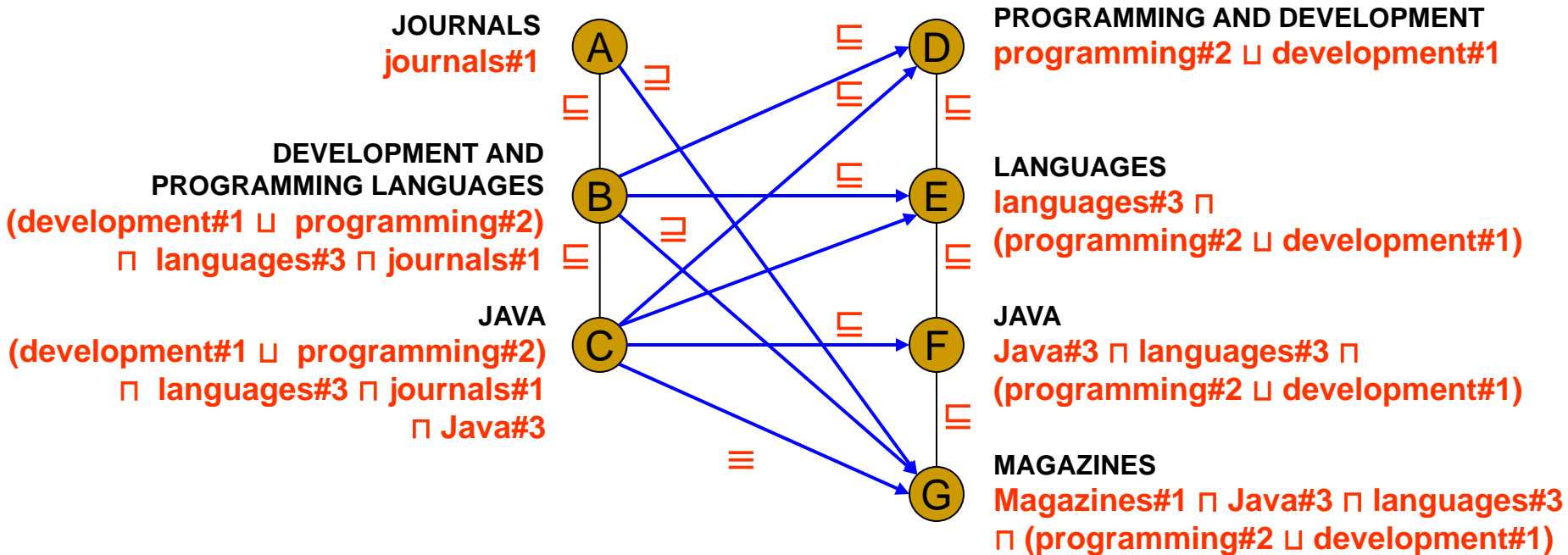
# Lightweight ontologies (formal classifications)

- We translate the graphs in input into **lightweight ontologies**
  - Node labels are formulas in propositional Description Logic (DL)
  - Concepts are taken from WordNet senses
  - Tree structures: each node formula is subsumed by parent node formula



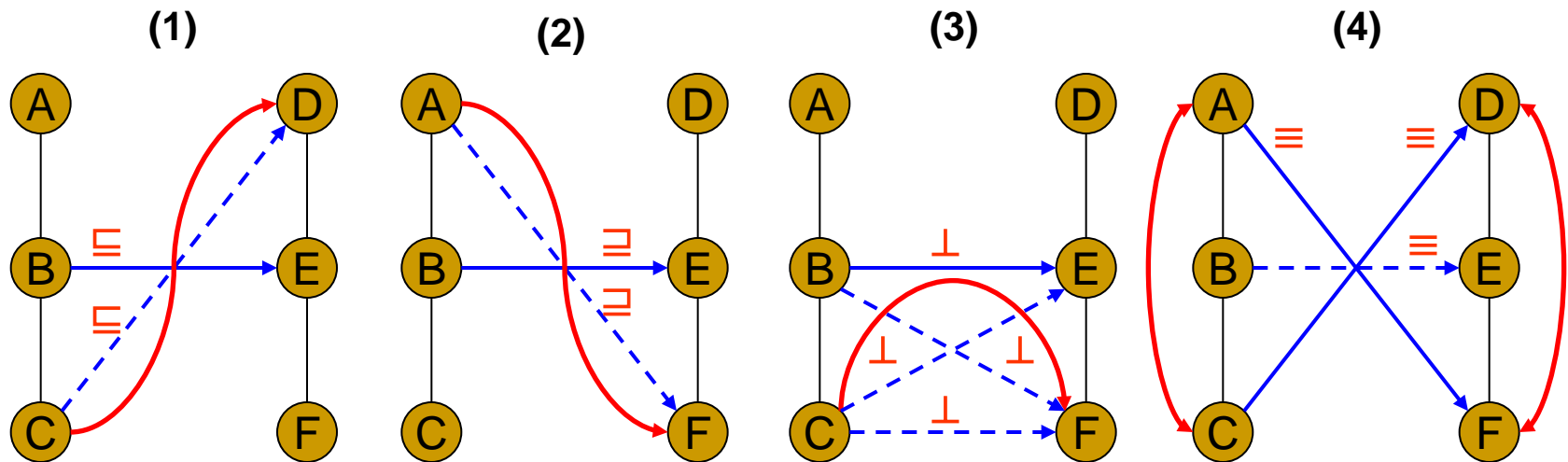
# Computing a mapping using SMatch

- A **Mapping** is a set of **mapping elements**  $\langle \text{source}, \text{target}, R \rangle$ 
  - $R \in \{ '\perp', '\equiv', '\sqsubseteq', '\supseteq' \}$  partially ordered
  - For each pair of nodes a call to a SAT solver verifies if a given semantic relation holds between the two, given the available background knowledge
  - Visualization and usability problems (e.g. validation and maintenance)



# Redundancy patterns

- We provide:
  - A definition of **redundant mapping element** (dashed arrows) based on the redundancy patterns below (redundancy w.r.t. another element).
  - A demonstration of soundness and completeness
- **Dependencies across-symbols**: equivalence is the combination of more and less specific
  - Pattern 4 can be seen as the combination of patterns 1 and 2
  - Patterns 1 and 2 are still valid in case of equivalence between B-E



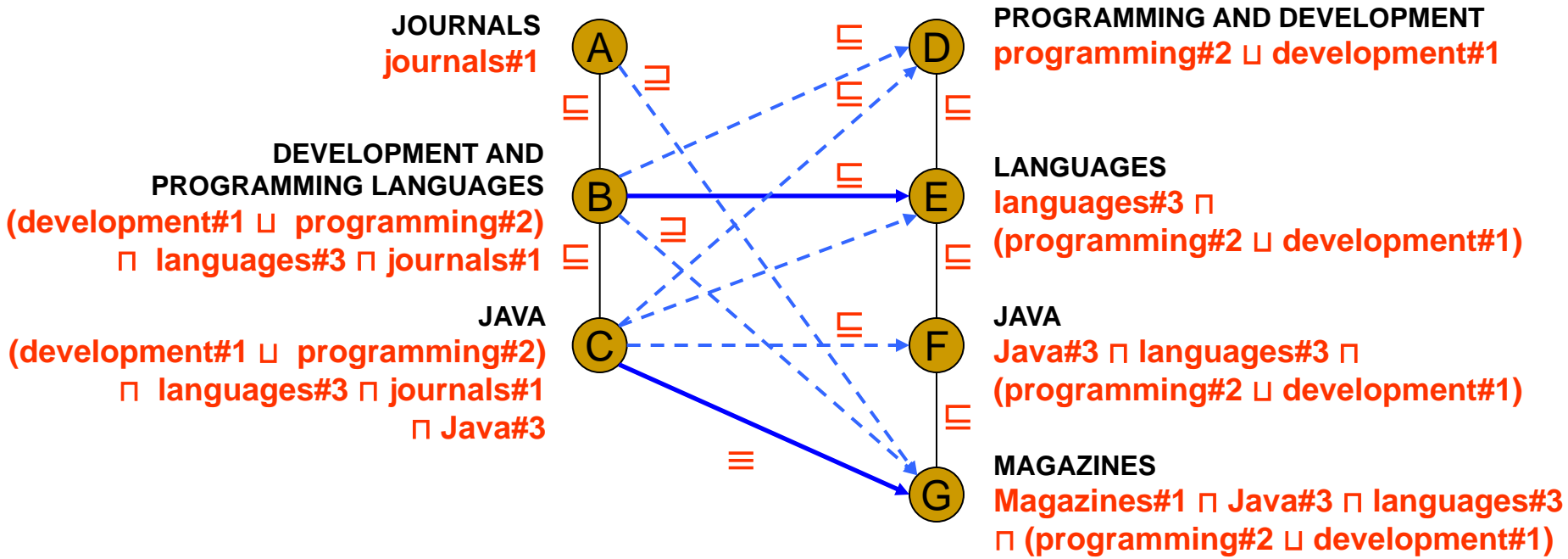
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# Minimal and redundant mappings

- We compute the **Minimal Mapping**
  - The subset of mapping elements of maximum size among those without redundant elements
  
- A **Redundant Mapping**
  - is a set containing redundant mapping elements
  
- The **Mapping of maximum size**
  - is the set containing the maximum number of mapping elements
  - It can be obtained from the propagation of the elements in the minimal set.

# MinSMatch: computing the minimal mapping

- The **minimal mapping** always exists and it is unique
- Advantages in visualization, validation and maintenance



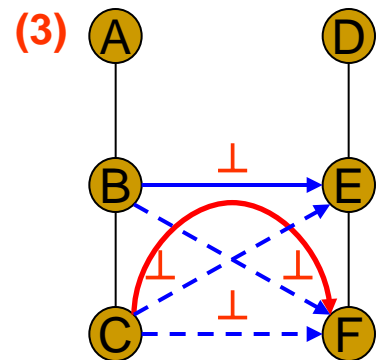
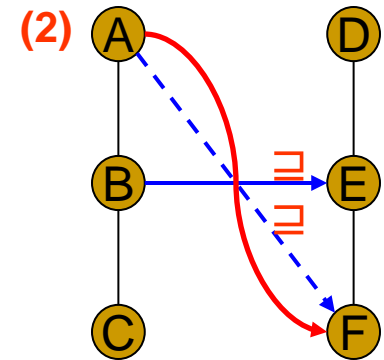
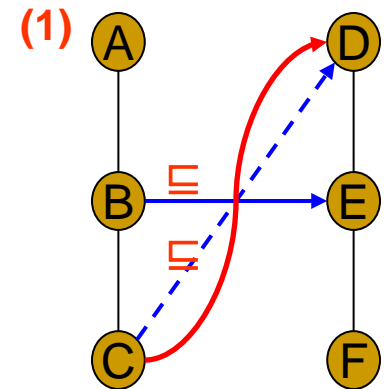
# MinSMatch: the algorithm

## Computing the minimal mapping M:

```
function TreeMatch(tree T1, tree T2) {  
  TreeDisjoint(root(T1),root(T2)); (3)  
  direction := true;  
  TreeSubsumedBy(root(T1),root(T2)); (1)  
  direction := false;  
  TreeSubsumedBy(root(T2),root(T1)); (2)  
  TreeEquiv(); (4) from (1) and (2)  
};
```

## Computing the set of maximum size:

```
function Propagate(M)
```





# MinSMatch: evaluation w.r.t. SMatch

- We evaluated it on 4 datasets of different dimensions:
  - 34 x 39 (University courses)
  - 542 x 999 (Art domain)
  - 2857 x 6628 (Web directories)
  - 3358 x 5239 (Business directories)
- SAT calls: 43-66% less
- Runtime: 16-59% less
- Size of the minimal mapping: 68-96% less
- Recall: up to 0.6% elements more (\*)

(\*) We minimize the problem of lack of background knowledge; the deeper the classifications the better.

The result of the propagation of the minimal set computed by MinSMatch is equivalent to the result of SMatch modulo inconsistencies.

# Conclusions

- The minimal mapping:
  - always exists and it is unique
  - offers usability advantages in visualization, validation and maintenance
- The MinSMATCH algorithm:
  - significantly faster w.r.t. SMATCH
  - efficiently computes the mapping of maximum size (by propagation)
  - increased recall (the deeper the classifications the better)
- Next steps:
  - Experimenting MinSMATCH on large scale knowledge organization systems (>400k nodes)
  - Avoid SAT
  - User interaction issues (navigation and validation tasks)

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# Questions



**Search on google and Wikipedia: Minimal mappings**

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